

1. a) greater b) smaller

2. a) three b) one fourth c) one ninth d) sixteen

$$3. \quad F = \frac{1}{4\pi\epsilon_0} \cdot \frac{Q_1 \cdot Q_2}{r^2} = \frac{1}{4\pi \cdot 8.85 \cdot 10^{-12} \frac{\text{C}^2}{\text{N} \cdot \text{m}^2}} \cdot \frac{1.6 \cdot 10^{-19} \text{ C} \cdot 1.6 \cdot 10^{-19} \text{ C}}{(2.0 \cdot 10^{-15} \text{ m})^2} = \underline{\underline{58 \text{ N}}}$$

$$4. \quad F = \frac{1}{4\pi\epsilon_0} \cdot \frac{Q_1 \cdot Q_2}{r^2} = \frac{1}{4\pi\epsilon_0} \cdot \frac{Q^2}{r^2}$$

$$Q = \sqrt{4\pi\epsilon_0 \cdot F \cdot r^2} = r \cdot \sqrt{4\pi\epsilon_0 \cdot F} = 0.025 \text{ m} \cdot \sqrt{4\pi \cdot 8.85 \cdot 10^{-12} \frac{\text{C}^2}{\text{N} \cdot \text{m}^2} \cdot 0.046 \text{ N}} = \underline{\underline{5.65 \cdot 10^{-8} \text{ C}}}$$

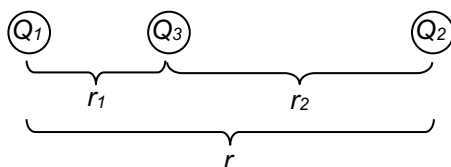
$$5. \quad \text{a) } F = \frac{1}{4\pi\epsilon_0} \cdot \frac{Q_1 \cdot Q_2}{r^2}$$

$$r = \sqrt{\frac{1}{4\pi\epsilon_0} \cdot \frac{Q_1 \cdot Q_2}{F}} = \sqrt{\frac{1}{4\pi \cdot 8.85 \cdot 10^{-12} \frac{\text{C}^2}{\text{N} \cdot \text{m}^2}} \cdot \frac{3.0 \cdot 10^{-8} \text{ C} \cdot 2.0 \cdot 10^{-8} \text{ C}}{0.0078 \text{ N}}} = \underline{\underline{2.6 \text{ cm}}}$$

b) The total charge amounts to +1.0 C. This charge is being distributed at equal parts between the two spheres (because they are the same size). Hence both spheres carry a charge of $+0.50 \cdot 10^{-8} \text{ C}$, repelling each other.

$$F = \frac{1}{4\pi\epsilon_0} \cdot \frac{Q_1 \cdot Q_2}{r^2} = \frac{1}{4\pi \cdot 8.85 \cdot 10^{-12} \frac{\text{C}^2}{\text{N} \cdot \text{m}^2}} \cdot \frac{0.50 \cdot 10^{-8} \text{ C} \cdot 0.50 \cdot 10^{-8} \text{ C}}{(0.026 \text{ m})^2} = \underline{\underline{3.3 \cdot 10^{-4} \text{ N}}}$$

6. a)



For Q_3 to be at equilibrium, the Coulomb force between Q_1 and Q_3 needs to be of the same magnitude as the Coulomb force between Q_2 and Q_3 . Let's assume all three charges to be positive:

$$F = \frac{1}{4\pi\epsilon_0} \cdot \frac{Q_1 \cdot Q_3}{r_1^2} = \frac{1}{4\pi\epsilon_0} \cdot \frac{Q_2 \cdot Q_3}{r_2^2} \Rightarrow \frac{Q_1}{r_1^2} = \frac{Q_2}{r_2^2} \Rightarrow \frac{Q}{r_1^2} = \frac{4Q}{r_2^2} \Rightarrow \frac{1}{r_1^2} = \frac{4}{r_2^2}$$

$$4 \cdot r_1^2 = r_2^2 \Rightarrow 2 \cdot r_1 = r_2$$

We use $r_1 + r_2 = r$ hence $2 \cdot r_1 = r - r_1 \Rightarrow r_1 = \underline{\underline{\frac{1}{3}r}}, r_2 = \underline{\underline{\frac{2}{3}r}}$