

9. a) $F_B = \rho_{\text{air}} \cdot g \cdot V_{\text{balloon}} = 1.293 \frac{\text{kg}}{\text{m}^3} \cdot 9.81 \frac{\text{m}}{\text{s}^2} \cdot 0.0050 \text{ m}^3 = 0.06342 \text{ N} = \underline{63 \text{ mN}}$

b) $F_G = F_G(\text{balloon}) + F_G(\text{filling})$

$$F_G(\text{filling}) = m_{\text{helium}} \cdot g = \rho_{\text{helium}} \cdot V_{\text{balloon}} \cdot g = 0.179 \frac{\text{kg}}{\text{m}^3} \cdot 0.0050 \text{ m}^3 \cdot 9.81 \frac{\text{m}}{\text{s}^2} = 0.00878 \text{ N} = 8.8 \text{ mN}$$

$$F_G = F_G(\text{balloon}) + F_G(\text{fillung}) = 30 \text{ mN} + 8.8 \text{ mN} = 38.8 \text{ mN} = \underline{39 \text{ mN}}$$

c) upward force = $F_B - F_G = 63.4 \text{ mN} - 38.8 \text{ mN} = \underline{25 \text{ mN}}$

10. $F_B = \rho_{\text{liquid}} \cdot V_{\text{immersed}} \cdot g = \rho_{\text{liquid}} \cdot V_{\text{displaced liquid}} \cdot g = m_{\text{displaced liquid}} \cdot g = F_G(\text{displaced liquid})$

11. sink

12. a) $F_B = \rho_{\text{water}} \cdot g \cdot V_{\text{immersed}} = 998 \frac{\text{kg}}{\text{m}^3} \cdot 9.81 \frac{\text{m}}{\text{s}^2} \cdot 0.000040 \text{ m}^3 = \underline{0.39 \text{ N}}$

b) 0.39 N (Archimedes' principle)

c) 0.39 N (If an object floats, the value of the buoyant force equals the value of the gravitational force)

d) $\rho_{\text{block}} = \frac{m_{\text{block}}}{V_{\text{block}}} = \frac{F_G(\text{block})}{g \cdot V_{\text{block}}} = \frac{0.39 \text{ N}}{9.81 \frac{\text{m}}{\text{s}^2} \cdot 0.0000500 \text{ m}^3} = \underline{795 \frac{\text{kg}}{\text{m}^3}}$

13. a) The cup floats and therefore we have: $F_B = F_G(\text{cup})$

$$\rho_{\text{water}} \cdot g \cdot V_{\text{immersed}} = m_{\text{cup}} \cdot g$$

$$V_{\text{immersed}} = \frac{m_{\text{cup}}}{\rho_{\text{water}}} = \frac{0.2000 \text{ kg}}{998 \frac{\text{kg}}{\text{m}^3}} = 0.000200 \text{ m}^3 = 0.200 \text{ dm}^3 = 200 \text{ cm}^3$$

$$h_{\text{immersed}} = \frac{V_{\text{immersed}}}{A} = \frac{200 \text{ cm}^3}{30.0 \text{ cm}^2} = \underline{6.67 \text{ cm}}$$

b) When the cup is immersed to its rim it is just about to sink. Its total volume is immersed.

$$F_A = F_G(\text{cup}) + F_G(\text{sand})$$

$$\rho_{\text{water}} \cdot g \cdot V_{\text{cup}} = m_{\text{cup}} \cdot g + m_{\text{sand}} \cdot g$$

$$m_{\text{sand}} = \rho_{\text{water}} \cdot V_{\text{cup}} - m_{\text{cup}} = 998 \frac{\text{kg}}{\text{m}^3} \cdot 0.000300 \text{ m}^3 - 0.200 \text{ kg} = 0.0994 \text{ kg} = \underline{99 \text{ g}}$$